A New Approach for Fluid Flow Model in Gas Tungsten Arc Weld Pool Using Longitudinal Electromagnetic Control

The mathematical model of body force incorporates the additional magnetic field influence in the weld pool

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ABSTRACT. In gas tungsten arc welding (GTAW), using a probe, the distribution of arc current density is measured with an additional longitudinal magnetic field. A model of the distribution of welding arc current flux is then modeled. Next, a new mathematical model of the body force is presented, which incorporates the additional influence of the magnetic field in the weld pool. Moreover, a model is developed for the fluid flow in the weld pool for the control process, which was based on experiments using LD10CS aluminum alloy. The boundary conditions are presented, and the influences of the additional longitudinal magnetic field and other factors are discussed using the equations describing the body forces.

Introduction

The arc welding technique that uses an additional electromagnetic field for control is called electromagnetic stirring. This technique is unlike standard arc welding techniques in that it offers the following advantages (Refs. 1–4):

- A low initial investment.
- An increase in operational reliability due to a high-performance coil.
- Higher mechanical quality from the fine crystal grain.
- A minimized risk of cold cracking because of the low hydrogen content.
- Exceptional appearance of the welding joints with clean weld surfaces.
- Increased environmental safety due to a lower magnetic field power.

This welding technique has a variety of applications in several fields, such as metallurgy, chemical engineering, manufacturing, electric power generation, aviation, and space flight (Refs. 2–8). Several aspects of welding with electromagnetic stirring have been analyzed previously.

Basic Theory

The application of the body force is not used in the standard GTAW process. The definition of the body force is the electromagnetic force applied to the fluid in the weld pool. It consists of the following two forces:

1) Self-electromagnetic force \( \mathbf{F}_m \) generated by the interaction of the divergent current and its self-induced magnetic field in the weld pool.

2) Additional electromagnetic force \( \mathbf{F}_w \) generated by the interaction of the divergent current and the additional longitudinal magnetic field in the weld pool.

Thus, the total electromagnetic force \( \mathbf{F}_m \) in the incompressible molten metal fluid of the GTA weld pool can be expressed as:

\[
\mathbf{F}_m = \mathbf{F}_m + \mathbf{F}_w \quad (1)
\]

When using longitudinal magnetic field control, the analysis of the body force is the key to understanding the fluid flow and heat transfer in the GTA weld pool. An analysis of the body force will assist in examining what effect an increase of the longitudinal magnetic field has on the GTA welding process. Therefore, the purpose of this paper is to define the body force and to model the fluid flow in the weld pool. In all the experiments, LD10CS aluminum alloy was used for simplicity and applicability.

Current Distribution

In direct current electrode negative (DCEN) GTAW undergoing additional longitudinal magnetic field control, a certain circumstance arises when using the nonmagnetic LD10CS aluminum alloy. The welding current flux density distribution on the surface of the weld pool is the same as the welding arc current flux density distribution on an interface between the welding arc and the weld pool. Thus, a probe method is used to measure the distribution of the welding arc current flux on this interface (Refs. 1, 4, 8). The experimental equipment used is shown in Fig. 1. The measurement values of the welding arc current flux distribution are shown in Fig. 2. These experiments were taken using a small welding current \( (I = 100 \, A) \) and weak magnetic field \( (B < 0.1 \, T) \).

The distribution character of the welding arc current flux can now be analyzed within these ranges of current and intensity of the magnetic field. A Gaussian distribution model of the welding arc current flux can be formulated using a numerical regression analysis as follows:

\[
j(r)_{arc} = j_0 \frac{K I}{\pi} \exp[-K(r)^2] \quad (3)
\]
where $j(r)_{arc}$ is the welding arc current flux distribution, $a$ is the lumped coefficient (generally between 0.5–3; in this paper $a = 1$) and $j_0$ is the current flux density.

$$K = \frac{a}{2\sigma_j}$$

is the form of the gather coefficient of current flux.

When the welding current is 100 A, the magnetic induction was 0.02 T and 0.05 T. The regression curves of welding arc current flux distribution are shown in Fig. 3. As shown, the measured values fit the proposed model of the welding arc current flux distribution.

**Body Force Equation**

The cylindrical coordinate system $(r, \theta, z)$ (see Fig. 4) is selected in order to derive the mathematical model of the body force in the GTA weld pool undergoing longitudinal magnetic field control. The vectors along the radial and axial directions, such as force, current flux, and magnetic induction, are expressed as two partial vectors $(r, z)$, respectively, and are symmetrical along the $z$-axis. Thus, the magnetic induction $B$ can be expressed as

$$\vec{B} = [0, B_0(r, z), 0] \quad (4)$$

Therefore, Equation 4 becomes

$$\langle \vec{B} \rangle = -\frac{1}{r} \frac{\partial \psi_e}{\partial z}, 0, \frac{1}{r} \frac{\partial \psi_e}{\partial r} \quad (7)$$

Because, in Equation 2, the term $\mu_0 j$ has the following form:

$$\mu_0 j = \mu_0 (j_r, 0, j_z) \quad (8)$$

After substitution of Equations 7 and 8 into Equation 2, the corresponding part of the vector can be expressed as

$$j_r = -\frac{1}{\mu_0} \frac{1}{r} \frac{f^2 \psi_e}{f r} \quad (9)$$

$$j_z = \frac{1}{\mu_0} \frac{1}{r} \frac{f^2 \psi_e}{f r}$$
Moreover,

\[
\tilde{j}(\tilde{B}) = \begin{cases} \epsilon, & \epsilon \neq 0 \\ 0, & \epsilon = 0 \end{cases}
\]

Moreover, when there is not electronic magnetic flow at the bottom of the welding workpiece. When the welding arc and workpiece.

\[
\frac{j}{\epsilon} = (-B_0j, 0, jB_0)
\]

According to Refs. 12–15, it is assumed that the electrical conductance is not temperature dependent. Thus,

\[
f_j = 0
\]

Therefore,

\[
f_j = \begin{cases} \frac{f_j}{f_z} = \frac{f}{f_z} \left( -\frac{1}{2} \frac{j_j}{\epsilon} \right) \\ \frac{1}{\epsilon} \frac{j_j}{f_z} = 0 \end{cases}
\]

where \(\psi_e = C_1z + C_2\)

Note when \(z = L\), then \(\psi_e = 0\) because there is not electronic magnetic flow at the bottom of the welding workpiece. When \(z = 0\), then

\[
\psi = \frac{f}{f_z} = \frac{j_j}{\epsilon}
\]

This is because the electronic magnetic flow on the surface of the welding workpiece (LD10CS aluminum alloy) is the same as the magnetic flow distribution of the welding arc on the interface between the welding arc and workpiece.

Thus, the magnetic flow function \(\psi_e\) becomes

\[
\psi|_{z=0} = \mu_0j|_{z=0} r dr
\]

Moreover, according to Fig. 2, Equation 3, and Equation 15, assuming a small current (\(I = 100\) A) and weak magnetic field (\(B < 0.1\) T), the boundary condition can be described as follows:

\[
\frac{j}{\epsilon}|_{z=0} = \frac{I}{2\pi\sigma_j} \left( -\frac{r^2}{2\sigma_j^2} \right)
\]

By solving the set of Equations 13, 14, and 17, the magnetic flow function \(\psi_e\) can be given as

\[
\psi_e = \frac{\frac{j}{\epsilon}}{2\pi\sigma_j} - \exp \left( -\frac{r^2}{2\sigma_j^2} \right) \frac{1 - z}{L}
\]

The current flux distribution of the GTA weld pool surface undergoing a longitudinal magnetic field is determined by the experimental measurement. Then the resulting (part something) is obtained from Fig. 2 and Equation 3.

Thus, Equation 6 can be expressed as

\[
B_0 = \psi_e = \frac{\mu_0j}{2\pi\sigma_j} - \exp \left( -\frac{r^2}{2\sigma_j^2} \right) \frac{1 - z}{L}
\]

After substituting Equation 18 into Equation 9, the current flux \(j\) of the LD10CS weld pool is given by

\[
j_z = \frac{I}{2\pi\sigma_j} \exp \left( -\frac{r^2}{2\sigma_j^2} \right) \frac{1 - z}{L}
\]

After substituting Equation 19 into Equation 11, Equation 11 can be expressed as

\[
\frac{j}{\epsilon} = \frac{I}{4\pi\sigma_j} \exp \left( -\frac{r^2}{2\sigma_j^2} \right) \frac{1 - z}{L}
\]

Then the self-electromagnetic force \(\vec{F}_{se}\) in the weld pool is as follows:

\[
\vec{F}_{se} = \frac{j}{\epsilon} \tilde{B}_z
\]

The additional electromagnetic force in the weld pool is expressed as follows:

\[
\vec{F}_{aw} = \frac{\mu_0j^2}{4\pi\sigma_j} \exp \left( -\frac{r^2}{2\sigma_j^2} \right) \frac{1 - z}{L}
\]

where \(\tilde{B}_z\) is the additional electromagnetic induction vector.

Therefore, the above formulations show that the electromagnetic force in the GTA weld pool undergoing a longitudinal magnetic field control (including the additional body force generated by the additional magnetic field) has polarity independence.

**Model of Fluid Flow**

Before introducing the mathematical model of fluid flow, certain definitions and assumptions need to be explained. There are three parts of the fluid velocity that are expressed as the radial velocity \((v)\), axial velocity \((u)\), and circumferential velocity \((w)\) in the directions of \(r, z,\) and \(\theta\), respectively (see Fig. 4). Moreover, there is an energy exchange, mass transfer, and heat transfer between the welding arc and the weld pool. Where the arc heat density \(q(r)\) and the current flux density \(\sigma_j\) are distributed on the surface of the welding workpiece, \(z = 0\). Lastly, the following conditions are assumed:

1) The surface of the weld pool is like a constant plane and the molten liquid metal in the weld pool is a Newton Body, which is a safe assumption when the arc welding current is less than 200 A.

2) The welding current is \(I < 200\) A and the magnetic field is \(B < 0.1\) T, where the distribution model of welding arc heating density and current flux have a Gaussian distribution.

As shown in Fig. 4, let \(u = u(r, z), v = v(r, z),\) and \(\omega = \omega(r, z)\) denote the velocity components in the axial \(z\) and radial \(r\) directions, respectively. The model of fluid flow would then be given as

\[
\frac{1}{r} \frac{f(rv) + f(w)}{f_z} = 0
\]
The fluid flow in the weld pool is governed by a combination of factors. In view of Equation 29 with regard to Equations 24, 25, and 27, the body force, electromagnetic force, and buoyant force can each be expressed as the following:

\[ F_z = -\frac{\mu_u I^2}{4\pi^2 \sigma r} \frac{1}{\xi} - \exp\left(-\frac{r^2}{2\sigma_l^2}\right) \]

\[ \left\langle 1 - \frac{z}{L} \right\rangle \rho \beta (T - T_i) \]  

(31)

\[ F_i = -\frac{\mu_u I^2}{4\pi^2 \sigma r} \exp\left(-\frac{r^2}{2\sigma_l^2}\right) \frac{1}{\xi} - \exp\left(-\frac{r^2}{2\sigma_l^2}\right) \left[1 - \frac{z}{L}\right]^2 \]

(32)

\[ F_b = \frac{a_0}{2\pi \sigma \xi} - \exp\left(-\frac{r^2}{2\sigma_j^2}\right) \]

(33)

**Boundary Condition**

For this model, the boundary conditions are ascertained from Equations 28–30 and are shown in Table 1. 

\[ Q_{arc} \quad \text{and} \quad Q_{loss} \quad \text{are defined as the heat input and heat loss, respectively. These terms are described as follows:} \]

\[ Q_{arc} = h_1(T - T_0) + S(T - T_0) \]  

(34)

\[ Q_{loss} = \frac{Q}{2\pi \sigma_{q_0}} \exp\left(-\frac{r^2}{2\sigma_{q_0}^2}\right) \]

\[ Q_{loss} = \eta (I U) \]  

(35)

(36)

\[ T = T_m \quad \text{at the liquid-solid boundary.} \]  

(37)

**Conclusion**

The welding properties for GTAW undergoing a longitudinal magnetic field control are different from the standard GTAW. The critical differences found from the research are summarized as follows:

1) The electromagnetic body forces in the weld pool include the self-electromagnetic force and the additional electromagnetic force. Also, the electromagnetic forces are independent of welding polarity. Moreover, by using a probe method, the current flux distribution on the surface of the LD10CS weld pool can be detected by measuring the arc current flux distribution. Then the welding arc current density distribution can be modeled. Finally, then the mathematical model of the body force in the LD10CS GTA weld pool undergoing a longitudinal magnetic field control is defined.

2) In addition, a new model of fluid flow in the weld pool was developed. This was done by examining the dynamics between the additional longitudinal magnetic field and the self-electromagnetic field, which accounts for the other body forces and the heat transferred. The boundary conditions were also provided. Thus, the model sufficiently described the electromagnetic field, the velocity field, and the thermal field on process. The model is, therefore, a comprehensive description for the fluid flow on GTA weld pool undergoing a longitudinal magnetic field.

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**List of Symbols**

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
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<tbody>
<tr>
<td>( \rho )</td>
<td>density (kg·m(^{-3}))</td>
</tr>
<tr>
<td>( P )</td>
<td>pressure (Pa)</td>
</tr>
<tr>
<td>( I )</td>
<td>welding current (A)</td>
</tr>
<tr>
<td>( j )</td>
<td>current flux density (A·m(^{-2}))</td>
</tr>
<tr>
<td>( B )</td>
<td>the magnetic induction (T)</td>
</tr>
<tr>
<td>( B_w )</td>
<td>additional magnetic induction (T)</td>
</tr>
<tr>
<td>( \sigma_w )</td>
<td>distribution parameter of current density (A·m(^{-2}))</td>
</tr>
<tr>
<td>( L )</td>
<td>thickness of workpiece (m)</td>
</tr>
<tr>
<td>( \beta )</td>
<td>coefficient of thermal expansion (K(^{-1}))</td>
</tr>
<tr>
<td>( g )</td>
<td>acceleration of gravity (m·s(^{-2}))</td>
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<tr>
<td>( T )</td>
<td>temperature (K)</td>
</tr>
<tr>
<td>( t )</td>
<td>time (s)</td>
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<tr>
<td>( C_p )</td>
<td>specific heat of workpiece (J·kg(^{-1})·K(^{-1}))</td>
</tr>
<tr>
<td>( T_m )</td>
<td>melting point of workpiece (K)</td>
</tr>
<tr>
<td>( \mu )</td>
<td>dynamic viscosity (kg·m(^{-1})·s)</td>
</tr>
<tr>
<td>( k )</td>
<td>thermal conductivity of molten metal (W·m(^{-1})·K(^{-1}))</td>
</tr>
<tr>
<td>( \delta )</td>
<td>thickness of workpiece (m)</td>
</tr>
<tr>
<td>( \mu_0 )</td>
<td>magnetic permeability (H·m(^{-1}))</td>
</tr>
<tr>
<td>( a_0 )</td>
<td>4\pi \times 10(^7) H/m</td>
</tr>
<tr>
<td>( T_0 )</td>
<td>initial temperature (K)</td>
</tr>
<tr>
<td>( h_c )</td>
<td>convection heat transfer coefficient (W·m(^{-2})·K(^{-1}))</td>
</tr>
<tr>
<td>( S )</td>
<td>Stefan-Boltzmann coefficient (W·m(^{-2})·K(^{-1}))</td>
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<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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<tbody>
<tr>
<td>( q_{loss} )</td>
<td>heat loss per unit time (W·m(^{-2}))</td>
</tr>
<tr>
<td>( q_{arc} )</td>
<td>heat input per unit time (W·m(^{-2}))</td>
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</table>

**References**

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